# Foundations of Algebra Teaching \& Learning Framework 

Semester 1

| Semester 1 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Module 1 <br> 2 weeks | Module 2 <br> 3 weeks | Module 3 <br> 3 weeks | Module 4 <br> 5 weeks | Module 5 <br> 5 weeks |
| Number Sense \& Quantity | Arithmetic to Algebra | Proportional Reasoning | Equations \& Inequalities | Quantitative Reasoning with Functions |
| MFANSQ1 <br> Relationships (4 operations; multiples of fractions; multiple/divide by powers of ten with decimals; compare fractions/decimals) MFANSQ2 +/(Real numbert- on a number line \& the meaning of zero) <br> MFANSQ3 Irrationals (Irrational number approximations; adding \& multiplying with rational \& irrational numbers) MFANSQ4 Computation (Compute multi-digit decimals; compute with rational numbers; division of fractions by fractions; multi-step problems with any form of rational number) <br> Algebra I Unit 1: MGSE9-12.N.RN. 3 (Properties of rational \& irrational numbers) | MFAAA1 Equivalent <br> Expressions (Commutative \& distributive properties; numerical \& algebraic expressions; add, subtract \& multiply algebraic expressions; equivalent expressions; evaluate formulas) <br> MFAAA2 Exponents (integer exponents; formulas; square \& cube roots; Pythagorean Theorem) <br> Algebra I Unit 1: <br> MGSE9-12.A.SSE. 1 <br> (Interpret expressions in context) <br> MGSE9-12.A.SSE.1a-b <br> (Interpret formulas \& expressions in context) MGSE9-12.A.APR. 1 <br> (Add, subtract \& multiply polynomials) <br> MGSE9-12.N.RN. 2 <br> (Expressions with Radicals) | MFAPR1 Equivalent Ratios (Equivalent ratios) MFAPR2 Proportions (Fraction equivalence \& division; percent problems) MFAPR3 Graphing (Unit rates as slope; similar triangles and slope; compare proportions in multiple representations) <br> Algebra I Unit 1: <br> MGSE9-12.N.Q.1-3 <br> (Reason quantitatively \& use units to solve problems) | MFAEI1 One Variable <br> (Solve equations \& inequalities \& justify solutions) <br> MFAEI2 Units <br> (Scale, units, graphing) <br> MFAEI3 Two Variables <br> (Algebraic models; graphing calculators; systems of equations) <br> MFAEI4 Literal Equations <br> (Solve for a specific variable) <br> Algebra I Unit 1: <br> MGSE9-12.N.Q.1-3 <br> (Reason quantitatively \& use units to solve problems) <br> Algebra I Unit 2: <br> MGSE9-12.A.CED.1-4 <br> (Create equations that describe numbers or relationships) <br> MGSE9-12.A.REI.1,3,5 <br> (Solve equations \& inequalities $1-2$ variable) <br> MGSE9-12.A.REI. 6 <br> (Solve systems) <br> MGSE9-12.A.REI.10-12 <br> (Solve equations \& inequalities $\mathbf{2}$ variables) | MFAQR1 Characteristics <br> (Domain \& range) <br> MFAQR2 Compare \& Graph <br> (Rates of change; linear \& non-linear; key features; compare with multiple representations) <br> MFAQR3 Construct \& Interpret <br> (Write; variables in context; function notation) <br> Algebra I Unit 2: <br> MGSE9-12.F.BF. 1 <br> (Write a function) <br> MGSE9-12.F.BF.1a,2 <br> (Arithmetic sequences) <br> MGSE9-12.F.IF. 1 <br> (Input vs. output) <br> MGSE9-12.F.IF. 2 <br> (Function notation) <br> MGSE9-12.F.IF.3-4 <br> (Sequences \& characteristics) <br> MGSE9-12.F.IF.5-6 <br> (Rate of change) <br> MGSE9-12.F.IF.7,7a,9 <br> (Analyze functions) |

 NSQ- number sense \& quantity
AA- arithmetic to algebra
PR- proportional reasoning
El- equations and inequalities
QR- quantitative reasoning with functions

## FA Algebra I Teaching \& Learning Framework

| Semester 2 |  |  |  |
| :---: | :---: | :---: | :---: |
| Unit 3 <br> 6 weeks | Unit 4 <br> 4 weeks | Unit 5 <br> 3 weeks | Unit 6 <br> 5 weeks |
| Modeling \& Analyzing Quadratic Functions | Modeling \& Analyzing Exponential Functions | Comparing \& Contrasting Functions | Describing Data Review and Extend |
| MGSE9-12.A.SSE. 2 <br> (Interpret the structure of expressions) <br> MGSE9-12.A.SSE.3,3a-b <br> (Equivalent forms of expressions) <br> MGSE9-12.A.CED.1-2,4 <br> (Create equations that describe numbers or relationships) <br> MGSE9-12.A.REI. 1 <br> (Justify how to solve an equation) <br> MGSE9-12.A.REI.4,4a-b <br> (Methods of solving quadratics) MGSE9-12.F.BF.1,3 <br> (Write a function \& build new functions) <br> MGSE9-12.F.IF. 1 <br> (Input vs. output) <br> MGSE9-12.F.IF. 2 <br> (Function notation) <br> MGSE9-12.F.IF. 4 <br> (Characteristics) <br> MGSE9-12.F.IF.5-6 <br> (Rate of change) <br> MGSE9-12.F.IF.7,7a <br> (Graph functions) <br> MGSE9-12.F.IF. 8 <br> (Write a function) <br> MGSE9-12.F.IF.8a,9 <br> (Compare \& contrast functions) | MGSE9-12.A.CED.1-2 <br> (Create equations 1-2 variables) MGSE9-12.A.REI. 1 <br> (Justify how to solve an equation) <br> MGSE9-12.F.BF. 1 <br> (Write a function) <br> MGSE9-12.F.BF.1a,2 <br> (Arithmetic \& geometric sequences) <br> MGSE9-12.F.BF. 3 <br> (Build new functions) <br> MGSE9-12.F.IF. 1 <br> (Input vs. output) <br> MGSE9-12.F.IF. 2 <br> (Function notation) <br> MGSE9-12.F.IF.3-4 <br> (Sequences \& characteristics) <br> MGSE9-12.F.IF.5-6 <br> (Rate of change) <br> MGSE9-12.F.IF.7,7e <br> (Graph functions) <br> MGSE9-12.F.IF. 9 <br> (Compare functions) | MGSE9-12.F.LE. 1 <br> (Linear vs exponential) <br> MGSE9-12.F.LE.1a <br> (Growth of functions) <br> MGSE9-12.F.LE.1b,c,2-3 <br> (Changes in rate and relating to context) <br> MGSE9-12.F.LE. 5 <br> (Interpret parameters) <br> MGSE9-12.F.BF. 3 <br> (Build new functions) <br> MGSE9-12.F.IF. 1 <br> (Input vs. output) <br> MGSE9-12.F.IF. 2 <br> (Function notation) <br> MGSE9-12.F.IF. 4 <br> (Characteristics) <br> MGSE9-12.F.IF.5-6 <br> (Rate of change) <br> MGSE9-12.F.IF. 7 <br> (Graph functions) <br> MGSE9-12.F.IF. 9 <br> (Compare functions) | MGSE9-12.S.ID. 1 <br> (Dot plots, histograms \& box plots) <br> MGSE9-12.S.ID. 2 <br> (Compare data distribution) MGSE9-12.S.ID. 3 <br> (Shape, center \& spread) <br> MGSE9-12.S.ID.5-6 <br> (Bivariate data) <br> MGSE9-12.S.ID.6a,c <br> (Function of best fit) <br> MGSE9-12.S.ID.7-9 <br> (Slope, correlation coefficient, causation \& correlation) <br> Review: All standards by differentiating for student needs <br> Extend: <br> MGSE9-12.G.CO. 1 <br> (Precise definitions) |


Grades 9-12 Key: Algebra Strand: SSE = Seeing Structure in Expressions, APR = Arithmetic with Polynomial and Rational Expressions, CED = Creating Equations, REI = Reasoning with Equations and Inequalities Functions Strand: IF = Interpreting Functions, LE = Linear and Exponential Models, BF = Building Functions, TF = Trigonometric Functions
Geometry Strand: CO = Congruence, SRT = Similarity, Right Triangles, and Trigonometry, C = Circles, GPE = Expressing Geometric Properties with Equations, GMD = Geometric Measurement and Dimension, MG = Modeling with Geometry
 Decisions

